

Beam Calculation



Relating to:

XXX

XXX

structural engineers & building surveyors

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Our registered office address is Ladbroke Farm, Banbury Road, Ladbroke, Warwickshire, CV47 2BY

The Institution of
StructuralEngineers

Project Preface

Client name:	xxx
Client address:	xxx
	xxx
	xxx

Prepared at:	Allcott Associates LLP 2 Victoria Works Vittoria Street Birmingham B1 3PE
Document prepared by:	James Bodicoat MEng CEng MICE MlstructE For and on behalf of Allcott Associates LLP

Date of Inspection:	xx/xx/xxxx
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Job reference:	xxxxxx
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1 Notes

1. The Building Contractors will need to, and must check all dimensions of openings on site prior to ordering steel, as we will not be held responsible for any incorrect lengths that are ordered.
2. Beams are designed to be the most economical size for the loading imposed in most cases, not for the thickness of wall above. It is therefore the contractor's responsibility to ensure that the load is correctly supported above the beam with a plate or other method.
3. The design is for the support Beam only and we are not responsible for ensuring the adequacy of any foundations beneath the supporting wall. This will generally be the responsibility of the Building Contractor to open up areas for the Building Inspector to verify. If we have to confirm foundation adequacy which is over and above the design an extra charge will be levied.
4. Should the length of the beams be revised by the client or the Building Contractor after we have completed our design which results in a redesign we reserve the right to charge again for all redesign works.
5. All dimensions used for design are clear openings only. Add a minimum 150mm bearing length to each end of beam unless otherwise stated for actual beam length when ordering beams
6. The designs are based on domestic loads only unless otherwise stated.
7. Changes to all drawings are at client's instructions. All drawings should be checked for accuracy and should not be scaled from. Any discrepancy should be immediately informed to Allcott Associates.
8. The design is for the steel beams only, not the foundation or additional width support on the beam for the wall or other above the beam.
9. This design does not mean that any other part of the building or than the beam itself complies with current building regulations and this should be checked with the local authority.
10. Unless otherwise stated pad stones should be proprietary precast C35 concrete 450mm long by 225 deep and 100mm wide.
11. Designs are based on client's instructions. If these are given incorrectly by the client and the design beam is not correct for the opening, this will not be the responsibility of this company. We reserve the right to charge again for any re-inspection and subsequent re-design.
12. The design will be based on the information including any drawings provided. Any opening up of areas will be the responsibility of the client. Any areas that are not opened up and are subsequently found not to be as informed to us by the Client and requires either a re-visit or re-calculation will be charged again.
13. The scope and any limitations to miscellaneous services will be agreed with you before commencing.
14. Should the configuration of the building change after the design of the beams which subsequently affect Part A of the Building regulations, which requires re-calculation and a revisit then this will be charged again.
15. It is the responsibility of the Building Contractors to ensure that all walls for the support of the beams are adequate for the correct support of the beams.
16. These calculations are for the sole use of the person instructing the design and cannot be passed to a third party without the consent of Allcott Associates as the content will not be guaranteed to be correct as to when the report was transferred.
17. These calculations are only valid for 6 months from the date of the survey as codes of practice change. If the practical works are commenced within that period you should check that the calculations are still valid.
18. All beams to be finished with red oxide paint and correctly fire protected.

2 Calculations Sheet

Reference:- 23 000

Date:- August 2019

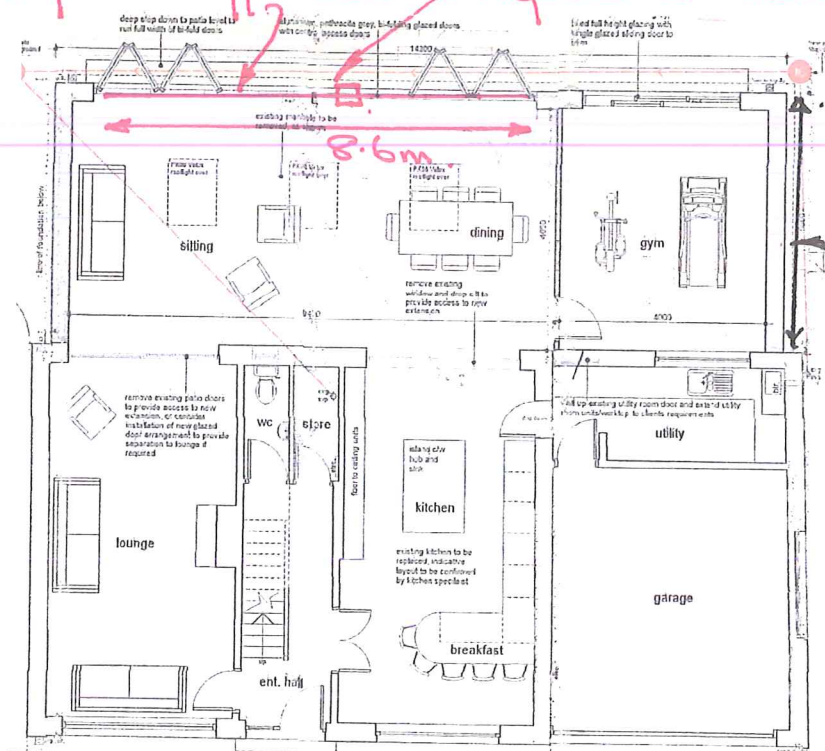
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Sheet No:- 1 of 4

ALLCOTT
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To provide support for roof above
Bifold doors in new Extension.

Proposed Support Beam Proposed Steel Column.



NOTE

Please Read The Notes Section
Ref:- Measurements

Plan
(NTS)

Section
(NTS)

FOR DESIGN

Factor of Safety Steel and Concrete 1.4 (Dead Load) + 1.6 (Imposed Load) + 1.0 (Other)
(To BS5628)

Factor of Safety Timber 1.0 (Dead Load) + 1.0 (Imposed Load) + 1.0 (Other)
(To BS5628)

Allowable Deflection $\delta = \text{Span} / 360$

Consider all Beams Un-Restrained

All Loadings to EN 1991 1-4

Please note

Beams are designed for Clear openings. Add the bearing length either side for the actual beam length

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STRUCTURAL ENGINEERS & SURVEYORS

Reference:- 23000

Date:- August 2019

Prepared By:- Eur. Ing. David J Allcott BSc(hons), CEng, CBuildE, MICE, MCABE, MIWEM, AssocRICS

Sheet No:- 2 of 4

Beam Design

Load from Roof: -/m run of beam.

dead $\frac{5.0}{2} \times 1.17 = 2.93 \text{ kN/m run}$

imposed $\frac{5.0}{2} \times 0.75 = 1.88 \text{ kN/m run}$

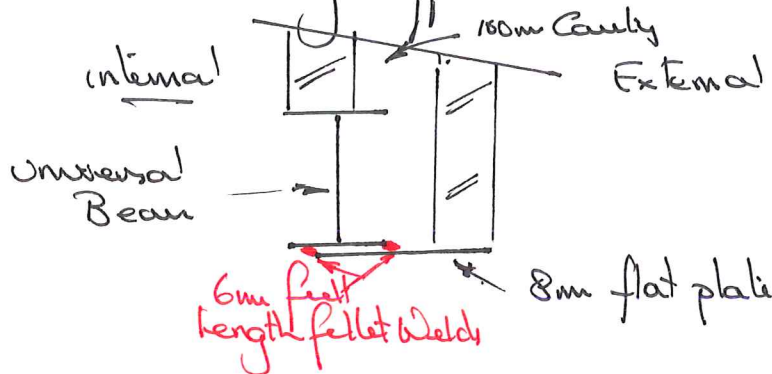
NOTE

Please Read The Notes Section

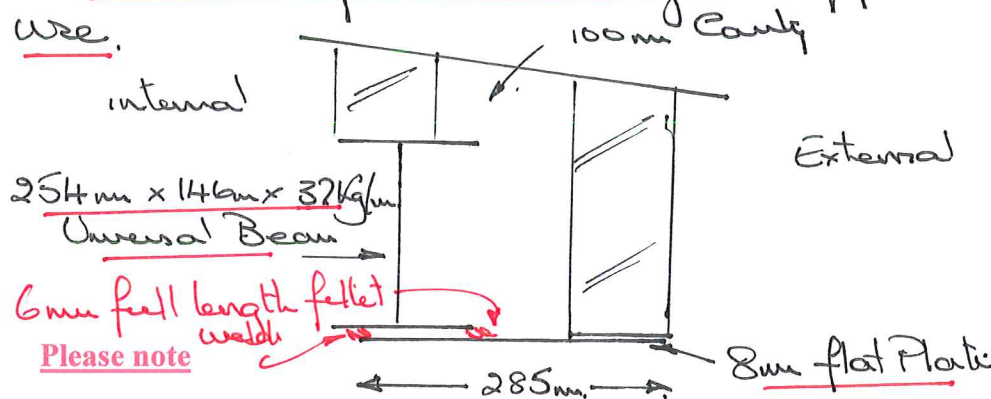
Ref:- Measurements

Loads used
dead - Roof tiles - 1.17 kN/m^2
imposed - Snow - 0.75 kN/m^2

Consider Trussing Support Beams



Consider 2 Beams, each 4.3m Clear Opening
∴ From Computer Analysis Appendix B1
use.



Please note

Beams are designed for Clear openings. Add the bearing length either side for the actual beam length

Reference:- 23000

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Sheet No:- 3 of 4



Column Design

NOTE

Please Read The Notes Section
Ref:- Measurements

From Previous Calculations

$$BTT = 21.7 \text{ kNm.}$$

$$\text{Shear} = 20.2 \text{ kN.}$$

$$\text{Axial Force} = 13.5 \text{ kN.}$$

∴ As 2 Beams Support on Column

$$\text{Use } BTT = 43.4 \text{ kNm.}$$

$$\text{Shear} = 40.4 \text{ kN.}$$

$$\text{Axial force} = 27 \text{ kN.}$$

∴ From Computer Analysis Appendix B2.

Use 120mm x 120mm x 10mm. (SHS)
(Square Hollow Section)

Please note

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Reference:- 23000

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Sheet No:- 4 of 4



Rafter Design.

Loads used

$$\text{dead} = 1.17 \text{ kN/m}^2.$$

$$\text{imposed} = 0.25 \text{ kN/m}^2.$$

Rafter Spacing 400mm.

Roof Slope - 11.5 degrees.

Length of Rafter on Slope 5.0m.

∴ From Computer Analysis Appendix B3.

Rafter will need to be.

$$\underline{250\text{mm} \times 47\text{mm C16 @ 400\text{mm}}}$$

NOTE

Please Read The Notes Section
Ref:- Measurements

Please note

Beams are designed for Clear openings. Add the bearing length either side for the actual beam length

3 Rights of Originator

We reserve the right to refuse copies of the report to any third party (other than those named above). We also reserve the right to amend our opinions in the event of additional information being made available at some future date. The Contracts (Rights of Third Parties) Act 1999 shall not apply to this agreement.

END OF REPORT

James Bodicoat MEng CEng MICE MstructE

For and on behalf of **Allcott Associates LLP**

Appendix A

Dead Loads

225mm Solid Wall	9"Brickwork	4.73 KN/m ²
	Plaster	0.20 KN/m ²
		<u>4.93 KN/m²</u>
250mm Cavity Wall	102 Brick	2.10 KN/m ²
	100 Block	1.35 KN/m ²
	Plaster	0.20 KN/m ²
		<u>3.65 KN/m²</u>
100mm Solid Wall	4"Brick	2.10 KN/m ²
	Plaster	0.20 KN/m ²
		<u>2.30 KN/m²</u>
Tiled Roof	Tiling/Battens/Felt	0.67 KN/m ²
	Timber	0.30 KN/m ²
	Ceiling/Insulation	0.20 KN/m ²
		<u>1.17 KN/m²</u>
1 st Floor	Floor joists, boarding	0.305 KN/m ²
	Finishes	0.050 KN/m ²
	Ceiling	0.20 KN/m ²
	Miscellaneous	0.15 KN/m ²
		<u>0.705 KN/m²</u>
Flat roof	Timbers / Felt Etc	0.42 KN/m ²
Ceiling	Plasterboard / Plaster	0.21 KN/m ²
Slate Roof	Slates/ Bath/ felt	0.28 KN/m ²
	Timber	0.30 KN/m ²
	Ceiling / Insulation	0.20 KN/m ²
		<u>0.78 KN/m²</u>

Imposed Loads

1 st Floor	1.50 KN/m ²
Flat Roof (no access)	0.75 KN/m ²
Pitched Roof	0.75 KN/m ²

Appendix B

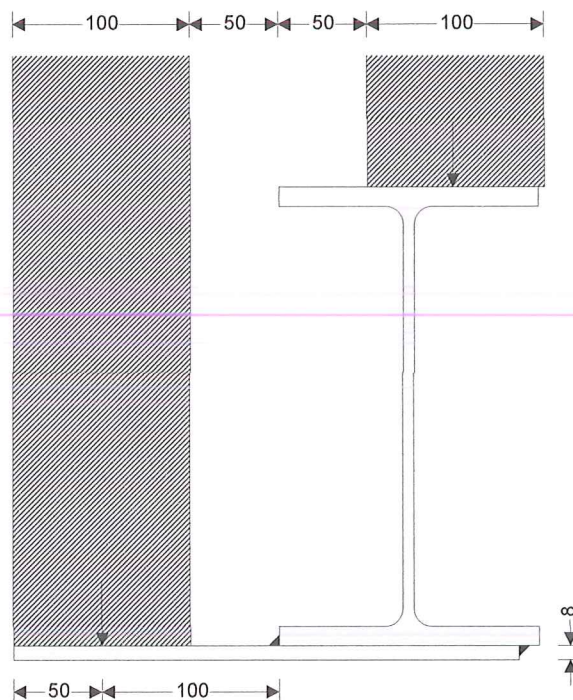
Project Holmfield, Bill lane, Woodale, Holmfirth, HD9 1XX				Job no. 23000	
Calcs for Masonry Support Beam				Start page no./Revision 1	
Calcs by DJA	Calcs date 08/08/2019	Checked by	Checked date	Approved by	Approved date

Appendix B1

STEEL MASONRY SUPPORT

In accordance with BS5950-1:2000 incorporating Corrigendum No.1

Tedds calculation version 1.0.04



Steel member details

Torsion beam

Masonry support plate

Steel grade of support plate

Design strength of support plate

Modulus of elasticity

Constant

Length of plate beyond beam

Total length of plate

Thickness of plate

Width of main beam

Area of plate

Distance from weld position to CoG

UB 254x146x37

User

S275

$p_{ysb} = 275 \text{ N/mm}^2$

$E = 205000 \text{ N/mm}^2$

$\epsilon = \sqrt{(275 \text{ N/mm}^2 / p_{ysb})} = 1.000$

$l_h = 150 \text{ mm}$

$l_{plate} = 285 \text{ mm}$

$t_{sb} = 8 \text{ mm}$

$B_{mb} = 146 \text{ mm}$

$A_{sbu} = t_{sb} \times l_{plate} = 2280.0 \text{ mm}^2$

$C_{ysb} = l_h / 2 - (l_{plate} - l_h) / 2 = 7 \text{ mm}$

Supported materials detail

Density of masonry on main beam

Width of masonry on main beam

Height of masonry on main beam

Eccentricity of main beam material

Add dead force main beam (not from masonry)

Add live force main beam (not from masonry)

Density of masonry on support beam

Width of masonry on support beam

Height of masonry on support beam

$\rho_{m,mb} = 20.0 \text{ kN/m}^3$

$b_{mmb} = 100 \text{ mm}$

$h_{mmb} = 134 \text{ mm}$

$e_{mb} = 50 \text{ mm}$


$P_{Gaddmb} = 2.9 \text{ kN/m}$

$P_{Qaddmb} = 1.9 \text{ kN/m}$

$\rho_{m,sb} = 20.0 \text{ kN/m}^3$

$b_{msb} = 100 \text{ mm}$

$h_{msb} = 400 \text{ mm}$

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			Approved by	Approved date

Add dead force support beam (not from masonry) $P_{Gaddsb} = 0.0 \text{ kN/m}$

Add live force support beam (not from masonry) $P_{Qaddsb} = 0.0 \text{ kN/m}$

Geometry

Cavity width $c = 100 \text{ mm}$

Supported width of masonry $d_m = l_h + e_{mb} - c = 100 \text{ mm}$

Biaxial stress effects in the plate (SCI-P-110)

Maximum overall bending moment $M_x = 21.7 \text{ kNm}$

Dist to NA combined section (CoG torsion beam) $y_{e,all} = (D_{mb} + t_{sb}) \times A_{sbu} / (2 \times (A_{mb} + A_{sbu})) = 43 \text{ mm}$

Second moment of area of combined section $I_{xx,all} = (I_{xxmb} + A_{mb} \times y_{e,all}^2) + A_{sbu} \times (D_{mb} / 2 + t_{sb} / 2 - y_{e,all})^2 = 8215 \text{ cm}^4$

Elastic section modulus of combined section $Z_{xx,all} = I_{xx,all} / (D_{mb} / 2 + t_{sb} - y_{e,all}) = 883.47 \text{ cm}^3$

Section modulus of plate $Z_{xx,plate} = 1m \times t_{sb}^2 / (6 \times 1m) = 10.67 \text{ cm}^3/m$

Eccentricity of support beam masonry $e_1 = 100 \text{ mm}$

Force of masonry on support plate $P_1 = (b_{msb} \times h_{msb} \times \rho_{m,sb} + P_{Gaddsb}) \times \gamma_{fG} + P_{Qaddsb} \times \gamma_{fQ} = 1.1 \text{ kN/m}$

Bending at heel $M_{x,plate} = P_1 \times e_1 = 0.1 \text{ kNm/m}$

Moment capacity of plate $M_c = 1.2 \times Z_{xx,plate} \times p_{ysb} = 3.5 \text{ kNm/m}$

PASS - Design strength exceeds stress at heel

Longitudinal stress due to overall bending $\sigma_1 = M_x / Z_{xx,all} = 24.5 \text{ N/mm}^2$

Constant relating to Von Mises curve $C_{fp} = (4 \times p_{ysb}^2 - 3 \times \sigma_1^2)^{0.5} = 548.4 \text{ N/mm}^2$

Transverse bending stress ratio limit $\alpha_{ts} = (C_{fp}^2 - \sigma_1^2) / (2 \times C_{fp} \times p_{ysb}) = 0.995$

Transverse bending stress ratio $\alpha_{ts} = M_{x,plate} / M_c = 0.032$

PASS - Transverse bending stress ratio less than allowable limit

Deflection at toe

Unfactored force on support angle $P_{1SLS} = b_{msb} \times h_{msb} \times \rho_{m,sb} + P_{Gaddsb} + P_{Qaddsb} = 0.8 \text{ kN/m}$

Distance from weld to load position $a_m = e_1 = 100 \text{ mm}$

Length of load resultant to edge of plate $b_m = l_h - e_1 = 50 \text{ mm}$

Dist from weld to load position as ratio of length $a_l = a_m / (a_m + b_m) = 0.667$

Effective second moment of inertia $I_{eff_def} = t_{sb}^3 / 12 = 42667 \text{ mm}^4/m$

Deflection at toe $\delta = (a_l^2 \times (3 - a_l) / 6) \times (P_{1SLS} \times (a_m + b_m)^3) / (E_{S5950} \times I_{eff_def}) = 0.05 \text{ mm}$

Deflection limit $\delta_{lim} = 2.00 \text{ mm}$

PASS - Deflection is within specified criteria

Weld details - assume a full length weld and that the plate acts as a propped cantilever with the prop at the weld position and the fixed end at the centre of the torsion beam

Leg length of weld $S_{weld} = 6 \text{ mm}$

Throat size of weld $a_{weld} = 1/\sqrt{2} \times S_{weld} = 4.2 \text{ mm}$

Shear force at weld position $R_A = P_1 \times \max((1 + (3 \times e_1) / (2 \times B_{mb} / 2)), 1.4) = 3.4 \text{ kN/m}$

Maximum possible force in plate $R_p = (l_h + B_{mb}) \times t_{sb} \times p_{ysb} = 652.1 \text{ kN}$

Longitudinal shear between beam and plate $R_l = 2 \times R_p / L = 303.3 \text{ kN/m}$

Horizontal shear between beam and plate $R_h = P_1 \times e_1 / (S_{weld} / 2 + t_{sb} / 2) = 16.0 \text{ kN/m}$

Resultant weld force $R_{weld} = (R_A^2 + R_l^2 + R_h^2)^{0.5} = 0.304 \text{ kN/mm}$

Strength of weld (Table 37) $p_{weld} = 220.0 \text{ N/mm}^2$


Capacity of full length weld $p_{c,weld} = a_{weld} \times p_{weld} = 0.933 \text{ kN/mm}$

PASS - Capacity of weld exceeds resultant force on weld

Torsional loading ULS

Loading of support beam masonry $w_{1ULS} = (h_{msb} \times b_{msb} \times \rho_{m,sb} + P_{Gaddsb}) \times \gamma_{fG} + P_{Qaddsb} \times \gamma_{fQ} = 1.12 \text{ kN/m}$

Loading of main beam masonry $w_{2ULS} = (h_{mmb} \times b_{mmb} \times \rho_{m,mb} + P_{Gaddmb}) \times \gamma_{fG} + P_{Qaddmb} \times \gamma_{fQ} = 7.49 \text{ kN/m}$

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Self weight of support beam

$$W_{3ULS} = A_{sbu} \times \rho_{sb} \times \gamma_{FG} = \mathbf{0.25 \text{ kN/m}}$$

Torsional loading SLS

Loading of support beam masonry

$$W_{1SLS} = h_{msb} \times b_{msb} \times \rho_{m, sb} + P_{Gaddsb} + P_{Qaddsb} = \mathbf{0.80 \text{ kN/m}}$$

Loading of main beam masonry

$$W_{2SLS} = h_{mmb} \times b_{mmb} \times \rho_{m, mb} + P_{Gaddmb} + P_{Qaddmb} = \mathbf{5.08 \text{ kN/m}}$$

Self weight of support beam

$$W_{3SLS} = A_{sbu} \times \rho_{sb} = \mathbf{0.18 \text{ kN/m}}$$

Eccentricities

Distance to shear centre of main beam

$$e_{0mb} = \mathbf{0 \text{ mm}}$$

Eccentricity of support beam masonry

$$e_{1mb} = (B_{mb} + b_{msb}) / 2 + c - e_{mb} = \mathbf{173 \text{ mm}}$$

Eccentricity of main beam masonry

$$e_{2mb} = (B_{mb} - b_{mmb}) / 2 - e_{mb} = \mathbf{-27 \text{ mm}}$$

Eccentricity of support beam

$$e_{3mb} = B_{mb} / 2 + c_{yysb} = \mathbf{81 \text{ mm}}$$

Torsional effects

Applied torque (ULS)

$$T_{qULS} = \text{abs}(W_{1ULS} \times e_{1mb} + W_{2ULS} \times e_{2mb} + W_{3ULS} \times e_{3mb}) = \mathbf{0.01 \text{ kNm/m}}$$

Total torque (ULS)

$$T_q = T_{qULS} \times L = \mathbf{0.06 \text{ kNm}}$$

Applied torque (SLS)

$$T_{qSLS} = \text{abs}(W_{1SLS} \times e_{1mb} + W_{2SLS} \times e_{2mb} + W_{3SLS} \times e_{3mb}) = \mathbf{0.02 \text{ kNm/m}}$$

Total torque (SLS)

$$T_{qu} = T_{qSLS} \times L = \mathbf{0.07 \text{ kNm}}$$

STEEL BEAM TORSION DESIGN

In accordance with BS5950-1:2000 incorporating Corrigendum No.1

Tedds calculation version 2.0.02

Section details

Section type

$$\text{UB } 254 \times 146 \times 37$$

Steel grade

$$\text{S275}$$

Design strength

$$p_{yw} = p_y = \mathbf{275 \text{ N/mm}^2}$$

Constant

$$\epsilon = \sqrt{(275 \text{ N/mm}^2 / p_y)} = \mathbf{1.000}$$

Geometry - Beam unrestrained against lateral-torsional buckling between supports.

Effective span

$$L = \mathbf{4300 \text{ mm}}$$

Length of segment for LT buckling

$$L_{LT} = \mathbf{5000 \text{ mm}}$$

Compression flanges laterally restrained

Both flanges free to rotate on plan

Effective length for LT buckling

$$L_{E,LT} = L_{LT} \times 1.0 = \mathbf{5000 \text{ mm}}$$

Loading - Torsional loading comprises only full-length uniformly distributed load(s)

Internal forces & moments on member under factored loading for uls design

Applied shear force

$$F_{vy} = \mathbf{20.2 \text{ kN}}$$

Maximum bending moment

$$M_{LT} = M_x = \mathbf{21.67 \text{ kNm}}$$

Applied torque

$$T_q = \mathbf{0.06 \text{ kNm}}$$

Minor axis bending moment

$$M_y = \mathbf{0 \text{ kNm}}$$

Compression force

$$F_c = \mathbf{0 \text{ kN}}$$

Equivalent uniform moment factors

EUM factor (Cl. 4.3.6.6 and T18)

$$m_{LT} = \mathbf{1.000}$$

Torsional deflection parameters


Beam is torsion fixed and warping free at each end. (as defined in SCI-P-057 section 2.1.6) - Appendix B case 4

Dist along the beam for first derivative of twist

$$z_1 = \mathbf{0 \text{ mm}}$$

Dist along the beam for second derivative of twist

$$z_2 = L / 2 = \mathbf{2150 \text{ mm}}$$

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First derivative of angle of twist

$$\phi'_1 = T_q / (G \times J) \times a / L \times [L^2 / (2 \times a) \times (1 / L - 2 \times z_1 / L^2) + \sinh(z_1 / a) - \tanh(L / (2 \times a)) \times \cosh(z_1 / a)] \times 1 \text{ rads} = \mathbf{1.14 \times 10^{-3} \text{ rads/m}}$$

Third derivative of angle of twist

$$\phi'''_1 = T_q / (G \times J \times a^2) \times a / L \times [\sinh(z_1 / a) - \tanh(L / (2 \times a)) \times \cosh(z_1 / a)] \times 1 \text{ rads} = \mathbf{-8.82 \times 10^{-4} \text{ rads/m}^3}$$

Angle of twist

$$\phi_2 = T_q \times a / (G \times J) \times a / L \times [L^2 / (2 \times a^2) \times (z_2 / L - z_2^2 / L^2) + \cosh(z_2 / a) - \tanh(L / (2 \times a)) \times \sinh(z_2 / a) - 1] \times 1 \text{ rads} = \mathbf{0.002 \text{ rads}}$$

Second derivative of angle of twist

$$\phi''_2 = T_q / (G \times J \times a) \times a / L \times [\cosh(z_2 / a) - \tanh(L / (2 \times a)) \times \sinh(z_2 / a) - 1] \times 1 \text{ rads} = \mathbf{-7.58 \times 10^{-4} \text{ rads/m}^2}$$

Design parameters

Total angle of twist

$$\phi = \text{abs}(\phi_2) = \mathbf{0.002 \text{ rads}}$$

First derivative of ϕ

$$\phi' = \text{abs}(\phi'_1) = \mathbf{1.14 \times 10^{-3} \text{ rads/m}}$$

Second derivative of ϕ

$$\phi'' = \text{abs}(\phi''_2) = \mathbf{7.58 \times 10^{-4} \text{ rads/m}^2}$$

Third derivative of ϕ

$$\phi''' = \text{abs}(\phi'''_1) = \mathbf{8.82 \times 10^{-4} \text{ rads/m}^3}$$

Section classification

$$b / T = \mathbf{6.7}$$

$$d / t = \mathbf{34.8}$$

$$r_{1s} = \min(1.0, \max(-1.0, F_c / (d \times t \times p_{yw}))) = \mathbf{0.000}$$

$$r_{2s} = F_c / (A_g \times p_{yw}) = \mathbf{0.000}$$

Section classification is plastic

Shear capacity (parallel to y-axis)

Design shear force

$$F_{vy} = \mathbf{20.2 \text{ kN}}$$

Design shear resistance (Cl. 4.2.3)

$$P_{vy} = 0.6 \times p_y \times A_{vy} = \mathbf{266.1 \text{ kN}}$$

Pass - Shear

Moment capacity (x-axis)

Design bending moment

$$M_x = \mathbf{21.7 \text{ kNm}}$$

Moment capacity

$$M_{cxu} = p_y \times S_x = \mathbf{132.9 \text{ kNm}}$$

Moment capacity low shear (Cl. 4.2.5.1)

$$M_{cx} = \min(p_y \times S_x, 1.2 \times p_y \times Z_x) = \mathbf{132.9 \text{ kNm}}$$

Pass - Moment capacity exceeds design bending moment

Lateral torsional buckling

Effective length for lateral torsional buckling

$$L_{E_LT} = \mathbf{5000 \text{ mm}}$$

Slenderness ratio

$$\lambda = L_{E_LT} / r_y = \mathbf{144}$$

Buckling parameter

$$u = \mathbf{0.890}$$

Flange ratio

$$\eta = \mathbf{0.5}$$

Torsional index

$$x = \mathbf{24.3}$$

Slenderness factor

$$v = 1 / (1 + 0.05 \times (\lambda / x)^2)^{0.25} = \mathbf{0.78}$$

Ratio - cl 4.3.6.9

$$\beta_w = 1.0 = \mathbf{1.000}$$

Equivalent slenderness - cl 4.3.6.7

$$\lambda_{LT} = u \times v \times \lambda \times \sqrt{\beta_w} = \mathbf{99}$$

Limiting slenderness - Annex B2.2

$$\lambda_{L0} = 0.4 \times \sqrt{\pi^2 \times E_{S5950} / p_y} = \mathbf{34}$$

Euler stress

$$p_E = \pi^2 \times E_{S5950} / \lambda_{LT}^2 = \mathbf{205 \text{ N/mm}^2}$$

Perry factor

$$\eta_{LT} = \max(7.0 \times (\lambda_{LT} - \lambda_{L0}) / 1000, 0) = \mathbf{0.455}$$


$$\phi_{LT} = (p_y + (\eta_{LT} + 1) \times p_E) / 2 = \mathbf{286606886.137}$$

Bending strength

$$p_b = p_E \times p_y / (\phi_{LT} + \sqrt{(\phi_{LT}^2 - p_E \times p_y)}) = \mathbf{126 \text{ N/mm}^2}$$

Buckling resistance moment

$$M_b = p_b \times S_x = \mathbf{60.9 \text{ kNm}}$$

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Max moment governing buckling resistance $M_{LT} = 21.7 \text{ kNm}$
Equiv uniform moment factor for LTB $m_{LT} = 1.00$
 $M_b / m_{LT} = 60.9 \text{ kNm}$

Pass - lat. tors. buckling

Buckling under combined bending & torsion -SCI-P-057 section 2.3

For simplicity, a conservative check is applied using the maximum stresses due to each of the separate load effects, even though these do not necessarily all occur at the same section along the member.

Span factor $L / a = 3.57$
Angle of twist $\phi = 0.002 \text{ rads}$
Second derivative of ϕ $\phi'' = 758. \times 10^{-6} \text{ rads/m}^2$
Induced minor axis moment $M_{yt} = M_x \times \phi / 1 \text{ rad} = 0.03 \text{ kNm}$
Normal stress at flange tip due to M_{yt} $\sigma_{byt} = M_{yt} / Z_y = 0 \text{ N/mm}^2$
Normal stress at flange tip due to warping $\sigma_w = E_{S5950} \times W_{n0} \times \phi'' / 1 \text{ rad} = 1 \text{ N/mm}^2$
Interaction index $i_b = M_x \times m_{LT} / M_b + (\sigma_{byt} + \sigma_w) / p_y \times (1 + 0.5 \times M_x \times m_{LT} / M_b) = 0.36$

Pass - Combined bending and torsion check satisfied

Local capacity under combined bending & torsion

For simplicity, a conservative check is applied using the maximum stresses due to each of the separate load effects, even though these do not necessarily all occur at the same section along the member.

Max. direct stress due to M_x $\sigma_{bx} = M_x / Z_x = 50 \text{ N/mm}^2$
Combined stress - eqn 2.22 $\sigma_{bx} + \sigma_{byt} + \sigma_w = 52 \text{ N/mm}^2$
Design strength $p_y = 275 \text{ N/mm}^2$

Pass - Local capacity

Combined shear stresses - SCI-P-057 section 2.3

For simplicity, a conservative check is applied using the maximum shear stresses due to each of the separate load effects, even though these do not necessarily all occur at the same section along the member.

Max shear stresses due to bending in web $\tau_{bw} = F_{vy} \times Q_w / (I_x \times t) = 14 \text{ N/mm}^2$
Max shear stresses due to bending in flange $\tau_{bf} = F_{vy} \times Q_f / (I_x \times T) = 3 \text{ N/mm}^2$
Max shear stresses due to torsion in web $\tau_{tw} = \text{abs}(G \times t \times \phi' / 1 \text{ rad}) = 1 \text{ N/mm}^2$
Max shear stresses due to torsion in flange $\tau_{tf} = \text{abs}(G \times T \times \phi' / 1 \text{ rad}) = 1 \text{ N/mm}^2$
Max shear stresses due to warping in flange $\tau_{wf} = \text{abs}(-E_{S5950} \times S_{w1} \times \phi''' / 1 \text{ rad} / T) = 0 \text{ N/mm}^2$
Amp shear stress torsion & warping in web $\tau_{vtw} = \tau_{tw} \times (1 + 0.5 \times M_x \times m_{LT} / M_b) = 1 \text{ N/mm}^2$
Amp shear stress torsion & warping in flange $\tau_{vtf} = (\tau_{tf} + \tau_{wf}) \times (1 + 0.5 \times M_x \times m_{LT} / M_b) = 1 \text{ N/mm}^2$

Combined shear stresses due to bending, torsion & warping:

Combined shear stresses in web $\tau_w = \tau_{bw} + \tau_{vtw} = 15 \text{ N/mm}^2$
Combined shear stresses in flange $\tau_f = \tau_{bf} + \tau_{vtf} = 4 \text{ N/mm}^2$
Shear strength $p_v = 0.6 \times p_y = 165 \text{ N/mm}^2$

Pass - Combined shear stresses

Twist check

Total applied torque (unfactored) $T_{qu} = 0.07 \text{ kNm}$
Maximum twist under sls loading $\phi_{sls} = \phi \times T_{qu} / T_q = 0.11 \text{ deg}$
Twist limit $\phi_{lim} = 1.00 \text{ deg}$

Pass - Twist

Deflection

Maximum y-axis deflection $\delta_{y_max} = 2.5 \text{ mm}$
Deflection limit - cl. 2.5.2 $\delta_{lim} = \min(L / k_{\delta}, \delta_{lim_abs}) = 3.0 \text{ mm}$



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Pass - Deflection within specified limit

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Appendix B2

STEEL COLUMN DESIGN

In accordance with EN1993-1-1:2005 incorporating Corrigenda February 2006 and April 2009 and the UK national annex

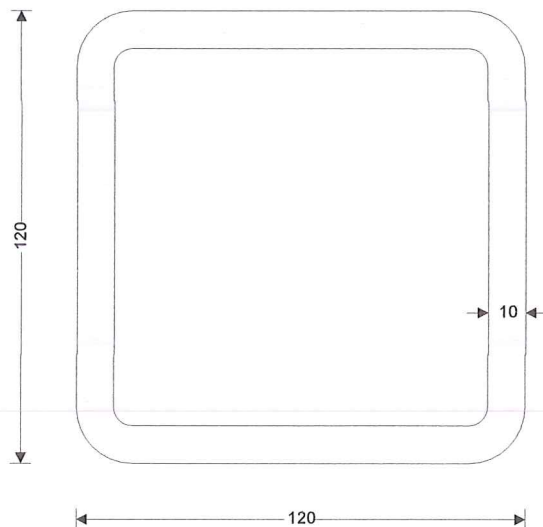
Tedds calculation version 1.1.04

Design summary

Description	Unit	Provided	Required	Utilisation	Result
Shear resistance (y-y)	kN	341	40	0.119	PASS
Axial compression	kN	1180	27	0.023	PASS
Bending resistance (y-y)	kNm	48	43	0.901	PASS
Combined bending & axial	kNm	48	43	0.901	PASS
Buckling in compression	kN	1029	27	0.026	PASS
Buckling in bending	kNm	48	43	0.901	PASS
Combined buckling				0.938	PASS

Partial factors - Section 6.1

Resistance of cross-sections $\gamma_{M0} = 1$
Resistance of members to instability $\gamma_{M1} = 1$
Resistance of cross-sections in tension to fracture $\gamma_{M2} = 1.1$



SHS 120x120x10.0 (Tata Steel Celsius)
Section depth, h, 120 mm
Section breadth, b, 120 mm
Mass of section, Mass, 33.7 kg/m
Section thickness, t, 10 mm
Area of section, A, 4293 mm²
Radius of gyration about y-axis, i_y , 44.555 mm
Radius of gyration about z-axis, i_z , 44.555 mm
Elastic section modulus about y-axis, $W_{el,y}$, 142025 mm³
Elastic section modulus about z-axis, $W_{el,z}$, 142025 mm³
Plastic section modulus about y-axis, $W_{pl,y}$, 175159 mm³
Plastic section modulus about z-axis, $W_{pl,z}$, 175159 mm³
Second moment of area about y-axis, I_y , 8521473 mm⁴
Second moment of area about z-axis, I_z , 8521473 mm⁴

Column details

Column section
Steel grade
Yield strength
Ultimate strength
Modulus of elasticity
Poisson's ratio
Shear modulus


SHS 120x120x10.0

S275

$f_y = 275 \text{ N/mm}^2$
 $f_u = 410 \text{ N/mm}^2$
 $E = 210 \text{ kN/mm}^2$
 $\nu = 0.3$
 $G = E / [2 \times (1 + \nu)] = 80.8 \text{ kN/mm}^2$

Column geometry

System length for buckling - Major axis $L_y = 2500 \text{ mm}$
System length for buckling - Minor axis $L_z = 2500 \text{ mm}$
The column is not part of a sway frame in the direction of the minor axis
The column is not part of a sway frame in the direction of the major axis

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Column loading

Axial load	$N_{Ed} = 27 \text{ kN (Compression)}$
Major axis moment at end 1 - Bottom	$M_{y,Ed1} = 43.4 \text{ kNm}$
Major axis moment at end 2 - Top	$M_{y,Ed2} = 43.4 \text{ kNm}$
	Major axis bending is single curvature
Minor axis moment at end 1 - Bottom	$M_{z,Ed1} = 0.0 \text{ kNm}$
Minor axis moment at end 2 - Top	$M_{z,Ed2} = 0.0 \text{ kNm}$
Major axis shear force	$V_{y,Ed} = 40 \text{ kN}$
Minor axis shear force	$V_{z,Ed} = 0 \text{ kN}$

Buckling length for flexural buckling - Major axis

End restraint factor	$K_y = 1.000$
Buckling length	$L_{cr,y} = L_y \times K_y = 2500 \text{ mm}$

Buckling length for flexural buckling - Minor axis

End restraint factor	$K_z = 1.000$
Buckling length	$L_{cr,z} = L_z \times K_z = 2500 \text{ mm}$

Web section classification (Table 5.2)

Coefficient depending on f_y	$\varepsilon = \sqrt{(235 \text{ N/mm}^2 / f_y)} = 0.924$
Depth between fillets	$c_w = h - 3 \times t = 90.0 \text{ mm}$
Ratio of c/t	$ratio_w = c_w / t = 9.00$
Length of web taken by axial load	$l_w = \min(N_{Ed} / (2 \times f_y \times t), c_w) = 4.9 \text{ mm}$
For class 1 & 2 proportion in compression	$\alpha = (c_w/2 + l_w/2) / c_w = 0.527$
Limit for class 1 web	$Limit_{1w} = (396 \times \varepsilon) / (13 \times \alpha - 1) = 62.53$

The web is class 1

Flange section classification (Table 5.2)

Depth between fillets	$c_f = b - 3 \times t = 90.0 \text{ mm}$
Ratio of c/t	$ratio_f = c_f / t = 9.00$
Limit for class 1 flange	$Limit_{1f} = 33 \times \varepsilon = 30.51$
Limit for class 2 flange	$Limit_{2f} = 38 \times \varepsilon = 35.13$
Limit for class 3 flange	$Limit_{3f} = 42 \times \varepsilon = 38.83$

The flange is class 1

Overall section classification

The section is class 1

Resistance of cross section (cl. 6.2)

Shear - Major axis (cl. 6.2.6)


Design shear force	$V_{y,Ed} = 40.4 \text{ kN}$
Shear area	$A_{vy} = A \times h / (b + h) = 2146 \text{ mm}^2$
Plastic shear resistance	$V_{pl,y,Rd} = A_{vy} \times (f_y / \sqrt{3}) / \gamma_{M0} = 340.8 \text{ kN}$
	$V_{y,Ed} / V_{pl,y,Rd} = 0.119$

PASS - Shear resistance exceeds the design shear force

$V_{y,Ed} \leq 0.5 \times V_{pl,y,Rd}$ - No reduction in f_y required for bending/axial force

Compression (cl. 6.2.4)

Design force	$N_{Ed} = 27 \text{ kN}$
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Design resistance

$$N_{c,Rd} = N_{pl,Rd} = A \times f_y / \gamma_{M0} = 1180 \text{ kN}$$

$$N_{Ed} / N_{c,Rd} = 0.023$$

PASS - The compression design resistance exceeds the design force

Bending - Major axis (cl. 6.2.5)

Design bending moment

$$M_{y,Ed} = \max(\text{abs}(M_{y,Ed1}), \text{abs}(M_{y,Ed2})) = 43.4 \text{ kNm}$$

Section modulus

$$W_y = W_{pl,y} = 175.2 \text{ cm}^3$$

Design resistance

$$M_{c,y,Rd} = W_y \times f_y / \gamma_{M0} = 48.2 \text{ kNm}$$

$$M_{y,Ed} / M_{c,y,Rd} = 0.901$$

PASS - The bending design resistance exceeds the design moment

Combined bending and axial force (cl. 6.2.9)

Ratio design axial to design plastic resistance

$$n = \text{abs}(N_{Ed}) / N_{pl,Rd} = 0.023$$

Ratio web area to gross area

$$a_w = \min(0.5, (A - 2 \times b \times t) / A) = 0.441$$

Ratio flange area to gross area

$$a_f = \min(0.5, (A - 2 \times h \times t) / A) = 0.441$$

Bending - Major axis (cl. 6.2.9.1)

Design bending moment

$$M_{y,Ed} = \max(\text{abs}(M_{y,Ed1}), \text{abs}(M_{y,Ed2})) = 43.4 \text{ kNm}$$

Plastic design resistance

$$M_{pl,y,Rd} = W_{pl,y} \times f_y / \gamma_{M0} = 48.2 \text{ kNm}$$

Modified design resistance

$$M_{N,y,Rd} = M_{pl,y,Rd} \times \min(1, (1 - n) / (1 - 0.5 \times a_w)) = 48.2 \text{ kNm}$$

$$M_{y,Ed} / M_{N,y,Rd} = 0.901$$

PASS - Bending resistance in presence of axial load exceeds design moment

Buckling resistance (cl. 6.3)

Yield strength for buckling resistance

$$f_y = 275 \text{ N/mm}^2$$

Flexural buckling - Major axis

Elastic critical buckling force

$$N_{cr,y} = \pi^2 \times E \times I_y / L_{cr,y}^2 = 2826 \text{ kN}$$

Non-dimensional slenderness

$$\bar{\lambda}_y = \sqrt{(A \times f_y / N_{cr,y})} = 0.646$$

Buckling curve (Table 6.2)

a

Imperfection factor (Table 6.1)

$$\alpha_y = 0.21$$

Parameter Φ

$$\Phi_y = 0.5 \times [1 + \alpha_y \times (\bar{\lambda}_y - 0.2) + \bar{\lambda}_y^2] = 0.756$$

Reduction factor

$$\chi_y = \min(1.0, 1 / [\Phi_y + \sqrt{(\Phi_y^2 - \bar{\lambda}_y^2)}]) = 0.872$$

Design buckling resistance

$$N_{b,y,Rd} = \chi_y \times A \times f_y / \gamma_{M1} = 1028.8 \text{ kN}$$

$$N_{Ed} / N_{b,y,Rd} = 0.026$$

PASS - The flexural buckling resistance exceeds the design axial load

Flexural buckling - Minor axis

Elastic critical buckling force

$$N_{cr,z} = \pi^2 \times E \times I_z / L_{cr,z}^2 = 2826 \text{ kN}$$

Non-dimensional slenderness

$$\bar{\lambda}_z = \sqrt{(A \times f_y / N_{cr,z})} = 0.646$$

Buckling curve (Table 6.2)

a

Imperfection factor (Table 6.1)

$$\alpha_z = 0.21$$

Parameter Φ

$$\Phi_z = 0.5 \times [1 + \alpha_z \times (\bar{\lambda}_z - 0.2) + \bar{\lambda}_z^2] = 0.756$$

Reduction factor

$$\chi_z = \min(1.0, 1 / [\Phi_z + \sqrt{(\Phi_z^2 - \bar{\lambda}_z^2)}]) = 0.872$$

Design buckling resistance

$$N_{b,z,Rd} = \chi_z \times A \times f_y / \gamma_{M1} = 1028.8 \text{ kN}$$

$$N_{Ed} / N_{b,z,Rd} = 0.026$$

PASS - The flexural buckling resistance exceeds the design axial load


Minimum buckling resistance

Minimum buckling resistance

$$N_{b,Rd} = \min(N_{b,y,Rd}, N_{b,z,Rd}) = 1028.8 \text{ kN}$$

$$N_{Ed} / N_{b,Rd} = 0.026$$

PASS - The axial load buckling resistance exceeds the design axial load

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Buckling resistance moment (cl.6.3.2.1)

Square hollow section not subject to lateral torsional buckling therefore:-


Reduction factor $\chi_{LT} = 1.0$
Design buckling resistance moment $M_{b,Rd} = \chi_{LT} \times W_y \times f_y / \gamma_{M1} = 48.2 \text{ kNm}$
Design bending moment $M_{y,Ed} = \max(\text{abs}(M_{y,Ed1}), \text{abs}(M_{y,Ed2})) = 43.4 \text{ kNm}$
 $M_{y,Ed} / M_{b,Rd} = 0.901$

PASS - The design buckling resistance moment exceeds the maximum design moment

Combined bending and axial compression (cl. 6.3.3)

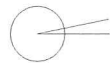
Characteristic resistance to normal force $N_{Rk} = A \times f_y = 1180 \text{ kN}$
Characteristic moment resistance - Major axis $M_{y,Rk} = W_{pl,y} \times f_y = 48.2 \text{ kNm}$
Characteristic moment resistance - Minor axis $M_{z,Rk} = W_{pl,z} \times f_y = 48.2 \text{ kNm}$
 $\psi_y = \text{if}(\text{abs}(M_{y,Ed1}) \leq \text{abs}(M_{y,Ed2}), M_{y,Ed1} / \text{if}(M_{y,Ed2} > 0 \text{ kNm}, \max(M_{y,Ed2}, 0.0001 \text{ kNm}), M_{y,Ed2}), M_{y,Ed2} / \text{if}(M_{y,Ed1} > 0 \text{ kNm}, \max(M_{y,Ed1}, 0.0001 \text{ kNm}), M_{y,Ed1})) = 1.000$
Moment distribution factor - Major axis $\psi_y = M_{y,Ed1} / M_{y,Ed2} = 1.000$
Moment factor - Major axis $C_{my} = \max(0.4, 0.6 + 0.4 \times \psi_y) = 1.000$
Moment distribution factor - Minor axis $\psi_z = M_{z,Ed1} / M_{z,Ed2} = 0.000$
Moment factor - Minor axis $C_{mz} = \max(0.4, 0.6 + 0.4 \times \psi_z) = 0.600$
Moment distribution factor for LTB $\psi_{LT} = M_{y,Ed1} / M_{y,Ed2} = 1.000$
Moment factor for LTB $C_{mLT} = \max(0.4, 0.6 + 0.4 \times \psi_{LT}) = 1.000$
Interaction factor $k_{yy} = C_{my} \times [1 + \min(0.8, \bar{\lambda}_y - 0.2) \times N_{Ed} / (\chi_y \times N_{Rk} / \gamma_{M1})] = 1.012$
Interaction factor $k_{zy} = 0.6 \times k_{yy} = 0.607$
Interaction factor $k_{zz} = C_{mz} \times [1 + \min(0.8, \bar{\lambda}_z - 0.2) \times N_{Ed} / (\chi_z \times N_{Rk} / \gamma_{M1})] = 0.607$
Interaction factor $k_{yz} = 0.6 \times k_{zz} = 0.364$
Section utilisation $UR_{B_1} = N_{Ed} / (\chi_y \times N_{Rk} / \gamma_{M1}) + k_{yy} \times M_{y,Ed} / (\chi_{LT} \times M_{y,Rk} / \gamma_{M1}) + k_{yz} \times M_{z,Ed} / (M_{z,Rk} / \gamma_{M1})$
 $UR_{B_1} = 0.938$
 $UR_{B_2} = N_{Ed} / (\chi_z \times N_{Rk} / \gamma_{M1}) + k_{zy} \times M_{y,Ed} / (\chi_{LT} \times M_{y,Rk} / \gamma_{M1}) + k_{zz} \times M_{z,Ed} / (M_{z,Rk} / \gamma_{M1})$
 $UR_{B_2} = 0.573$

PASS - The buckling resistance is adequate

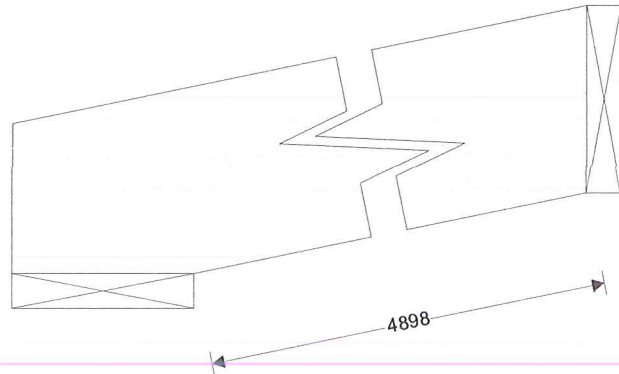
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TIMBER RAFTER DESIGN (BS5268-2:2002)

Appendix B3
TEDDS calculation version 1.0.03



12 degrees



Rafter details

Breadth of timber sections
Depth of timber sections
Rafter spacing
Rafter slope
Clear span of rafter on horizontal
Clear span of rafter on slope
Rafter span
Timber strength class

$b = 47 \text{ mm}$
 $h = 250 \text{ mm}$
 $s = 400 \text{ mm}$
 $\alpha = 11.5 \text{ deg}$
 $L_{clh} = 4800 \text{ mm}$
 $L_{cl} = L_{clh} / \cos(\alpha) = 4898 \text{ mm}$
Single span
C16

Section properties

Cross sectional area of rafter
Section modulus
Second moment of area
Radius of gyration

$A = b \times h = 11750 \text{ mm}^2$
 $Z = b \times h^2 / 6 = 489583 \text{ mm}^3$
 $I = b \times h^3 / 12 = 61197917 \text{ mm}^4$
 $r = \sqrt{I / A} = 72.2 \text{ mm}$

Loading details

Rafter self weight
Dead load on slope
Imposed load on plan
Imposed point load

$F_j = b \times h \times \rho_{char} \times g_{acc} = 0.04 \text{ kN/m}$
 $F_d = 1.15 \text{ kN/m}^2$
 $F_u = 0.75 \text{ kN/m}^2$
 $F_p = 0.90 \text{ kN}$

Modification factors

Section depth factor
Load sharing factor

$K_7 = (300 \text{ mm} / h)^{0.11} = 1.02$
 $K_8 = 1.10$

Consider long term load condition


Load duration factor
Total UDL perpendicular to rafter
Notional bearing length
Effective span

$K_3 = 1.00$
 $F = F_d \times \cos(\alpha) \times s + F_j \times \cos(\alpha) = 0.486 \text{ kN/m}$
 $L_b = F \times L_{cl} / [2 \times (b \times \sigma_{cp1} \times K_8 - F)] = 11 \text{ mm}$
 $L_{eff} = L_{cl} + L_b = 4909 \text{ mm}$

Check bending stress

Bending stress parallel to grain
Permissible bending stress
Applied bending stress

$\sigma_m = 5.300 \text{ N/mm}^2$
 $\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 5.948 \text{ N/mm}^2$
 $\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) = 2.989 \text{ N/mm}^2$

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PASS - Applied bending stress within permissible limits

Check compressive stress parallel to grain

Compression stress parallel to grain	$\sigma_c = 6.800 \text{ N/mm}^2$
Minimum modulus of elasticity	$E_{min} = 5800 \text{ N/mm}^2$
Compression member factor	$K_{12} = 0.60$
Permissible compressive stress	$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 4.476 \text{ N/mm}^2$
Applied compressive stress	$\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) = 0.561 \text{ N/mm}^2$

PASS - Applied compressive stress within permissible limits

Check combined bending and compressive stress parallel to grain

Euler stress	$\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 12.373 \text{ N/mm}^2$
Euler coefficient	$K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.959$
Combined axial compression and bending check	$\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.649 < 1$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain	$\tau = 0.670 \text{ N/mm}^2$
Permissible shear stress	$\tau_{adm} = \tau \times K_3 \times K_8 = 0.737 \text{ N/mm}^2$
Applied shear stress	$\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) = 0.152 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

Check deflection

Permissible deflection	$\delta_{adm} = 0.003 \times L_{eff} = 14.727 \text{ mm}$
Bending deflection	$\delta_b = 5 \times F \times L_{eff}^4 / (384 \times E_{mean} \times I) = 6.820 \text{ mm}$
Shear deflection	$\delta_s = 12 \times F \times L_{eff}^2 / (5 \times E_{mean} \times A) = 0.272 \text{ mm}$
Total deflection	$\delta_{max} = \delta_b + \delta_s = 7.091 \text{ mm}$

PASS - Total deflection within permissible limits

Consider medium term load condition

Load duration factor	$K_3 = 1.25$
Total UDL perpendicular to rafter	$F = [F_u \times \cos(\alpha)^2 + F_d \times \cos(\alpha)] \times s + F_j \times \cos(\alpha) = 0.774 \text{ kN/m}$
Notional bearing length	$L_b = F \times L_{cl} / [2 \times (b \times \sigma_{cp1} \times K_8 - F)] = 17 \text{ mm}$
Effective span	$L_{eff} = L_{cl} + L_b = 4915 \text{ mm}$

Check bending stress

Bending stress parallel to grain	$\sigma_m = 5.300 \text{ N/mm}^2$
Permissible bending stress	$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 7.435 \text{ N/mm}^2$
Applied bending stress	$\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) = 4.773 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits


Check compressive stress parallel to grain

Compression stress parallel to grain	$\sigma_c = 6.800 \text{ N/mm}^2$
Minimum modulus of elasticity	$E_{min} = 5800 \text{ N/mm}^2$
Compression member factor	$K_{12} = 0.56$
Permissible compressive stress	$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 5.196 \text{ N/mm}^2$
Applied compressive stress	$\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) = 0.894 \text{ N/mm}^2$

PASS - Applied compressive stress within permissible limits

Check combined bending and compressive stress parallel to grain

Euler stress	$\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 12.341 \text{ N/mm}^2$
Euler coefficient	$K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.940$

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	Calcs by DJA	Calcs date 08/08/2019	Checked by	Checked date	Approved by	Approved date

Combined axial compression and bending check $\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.855 < 1$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain

$$\tau = 0.670 \text{ N/mm}^2$$

Permissible shear stress

$$\tau_{adm} = \tau \times K_3 \times K_8 = 0.921 \text{ N/mm}^2$$

Applied shear stress

$$\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) = 0.243 \text{ N/mm}^2$$

PASS - Applied shear stress within permissible limits

Check deflection

Permissible deflection

$$\delta_{adm} = 0.003 \times L_{eff} = 14.745 \text{ mm}$$

Bending deflection

$$\delta_b = 5 \times F \times L_{eff}^4 / (384 \times E_{mean} \times I) = 10.920 \text{ mm}$$

Shear deflection

$$\delta_s = 12 \times F \times L_{eff}^2 / (5 \times E_{mean} \times A) = 0.434 \text{ mm}$$

Total deflection

$$\delta_{max} = \delta_b + \delta_s = 11.354 \text{ mm}$$

PASS - Total deflection within permissible limits

Consider short term load condition

Load duration factor

$$K_3 = 1.50$$

Total UDL perpendicular to rafter

$$F = F_d \times \cos(\alpha) \times s + F_j \times \cos(\alpha) = 0.486 \text{ kN/m}$$

Notional bearing length

$$L_b = [F \times L_{cl} + F_p \times \cos(\alpha)] / [2 \times (b \times \sigma_{cp1} \times K_8 - F)] = 14 \text{ mm}$$

Effective span

$$L_{eff} = L_{cl} + L_b = 4913 \text{ mm}$$

Check bending stress

Bending stress parallel to grain

$$\sigma_m = 5.300 \text{ N/mm}^2$$

Permissible bending stress

$$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 8.922 \text{ N/mm}^2$$

Applied bending stress

$$\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) + F_p \times \cos(\alpha) \times L_{eff} / (4 \times Z) = 5.206 \text{ N/mm}^2$$

PASS - Applied bending stress within permissible limits

Check compressive stress parallel to grain

Compression stress parallel to grain

$$\sigma_c = 6.800 \text{ N/mm}^2$$

Minimum modulus of elasticity

$$E_{min} = 5800 \text{ N/mm}^2$$

Compression member factor

$$K_{12} = 0.52$$

Permissible compressive stress

$$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 5.781 \text{ N/mm}^2$$

Applied compressive stress

$$\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) + F_p \times \sin(\alpha) / A = 0.576 \text{ N/mm}^2$$

PASS - Applied compressive stress within permissible limits

Check combined bending and compressive stress parallel to grain

Euler stress

$$\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 12.353 \text{ N/mm}^2$$

Euler coefficient

$$K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.964$$

Combined axial compression and bending check

$$\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.705 < 1$$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain

$$\tau = 0.670 \text{ N/mm}^2$$

Permissible shear stress

$$\tau_{adm} = \tau \times K_3 \times K_8 = 1.106 \text{ N/mm}^2$$

Applied shear stress

$$\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) + 3 \times F_p \times \cos(\alpha) / (2 \times A) = 0.265 \text{ N/mm}^2$$

PASS - Applied shear stress within permissible limits

Check deflection

Permissible deflection


$$\delta_{adm} = 0.003 \times L_{eff} = 14.738 \text{ mm}$$

Bending deflection

$$\delta_b = L_{eff}^3 \times (5 \times F \times L_{eff} / 384 + F_p \times \cos(\alpha) / 48) / (E_{mean} \times I) = 10.887 \text{ mm}$$

Shear deflection

$$\delta_s = 12 \times L_{eff} \times (F \times L_{eff} + 2 \times F_p \times \cos(\alpha)) / (5 \times E_{mean} \times A) = 0.473 \text{ mm}$$

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Total deflection

$\delta_{max} = \delta_b + \delta_s = 11.360 \text{ mm}$

PASS - Total deflection within permissible limits

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